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Investigation of Initial Lithiation of Silicon (100) Using Solid-State ⁷Li NMR

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Structural changes in amorphous Li_xSi during the initial lithiation of single crystal Si to amorphous Li_xSi were investigated as a function of Li flux and total charge using solid-state ⁷Li nuclear magnetic resonance (NMR) spectroscopy. Single crystal (100) Si wafers were used as a model system in this study, as the Li flux could be precisely controlled and uniformly distributed across the surface of the wafer. It was observed that peak shifts in solid-state ⁷Li NMR spectra varied as a function of the Li flux during the initial lithiation and stayed constant for samples of the same Li flux regardless of the total charge applied to the electrodes. We conclude from these results that the Li concentration in Li_xSi stays constant for a given flux regardless of the total coulombic charge applied to the electrode. The results from this study help better understand the kinetics, the reaction mechanisms, and the kinetic modeling of chemical reactions at the reaction front during the initial lithiation of Si (100). (© 2014 The Electrochemical Society. [DOI: 10.1149/2.033406jes] All rights reserved.

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Silicon, Si, is a promising anode material for use in lithiumion secondary batteries thanks to its large charge capacity,¹ natural abundance and the availability of state-of-the-art fabrication methods. However, performance degradation stemming from mechanical damage driven by colossal volumetric expansion^{1,2} has prevented practical uses of Si-based anodes, though many methods for the improvement of Si anode performances³⁻¹⁰ have been proposed. Numerous experimental and theoretical studies have provided extensive understanding of the lithiation and delithiation process of crystalline Si to amorphous Li_xSi (where x is the ratio of Li to Si atoms), includ-ing phase transformation,^{11–15} kinetics,^{16–22} mechanical stress and deformation,^{23,24} etc. First principle calculations^{11,12} predicted that a very small number (x = $0.2 \sim 0.3$) of Li atoms could drive the crystalline-to-amorphous phase transition. An in-situ X-ray diffraction (XRD) study¹⁵ showed that an amorphous phase of Li_xSi with a fixed Li concentration of $x \sim 3.5$ is formed during the initial lithiation of crystalline silicon particles. The fixed Li concentration of $x \sim 3.5$ has been widely accepted in many published studies.^{15–17,24–26} Jung, et al.¹⁷ also predicted energetically favorable Li concentration of Li_{3,4}Si at the amorphous-crystalline interface by employing first-principles molecular dynamics simulations. Chon, et al.²⁴ directly observed morphologies of crystalline and amorphous phases and their sharp (~ 1 nm) phase boundary in an electrochemically lithiated single crystal Si wafer by transmission electron microscopy (TEM). Phase transformation, co-existence of crystalline and amorphous phases and a moving phase boundary toward the crystalline silicon phase were considered as essential elements to describe the kinetics¹⁶ for the initial lithiation of crystalline silicon assuming a constant Li concentration of a fixed structure of Li3.5Si.

The kinetics of the initial lithiation of crystalline silicon comprise of three processes in series: (i) the redox reaction at the electrolyte/lithiated silicon interface; (ii) the diffusion of lithium through the lithiated phase; (iii) the chemical reaction at the interface between lithiated and crystalline silicon, known as the reaction front. It was found that the chemical reaction at the reaction front is a rate limiting process for the initial lithiation of crystalline silicon,¹⁶ but there is a lack of experimental data for the modeling of kinetics at the reaction front. Therefore, the information on structural changes in Li_xSi as a function of Li flux and total charge is essential for a better understanding of kinetics and reaction mechanism at the reaction front. Nuclear magnetic resonance (NMR) spectroscopy is a powerful technique for probing local structures of interest, even in a disordered system because it is extremely sensitive to the local magnetic field around nuclei at an atomic scale. Previous in-situ and ex-situ solid-state ⁷Li NMR studies^{26–31} on micro- and nano-sized crystalline Si anodes provided information on the local structure of both crystalline and amorphous lithium silicides. Key et al.²⁶ determined local structures of amorphous Li_xSi formed during the initial lithiation of micro crystalline Si particles using distinct characteristic NMR chemical shifts of known crystalline lithium silicides as references. In both previous NMR studies,^{26,27} multiple nuclear magnetic resonances corresponding to different amorphous Li_xSi structures were observed at a given lithiation condition.

Since micro and nano-crystalline Si electrodes were used in previous NMR^{26,27} and XRD¹⁵ studies, the current density (defined as Li flux in μ A/cm²) is not uniform on all particles due to varying particle sizes, shapes and distances from particles to the current collector. In addition, the area of phase boundary decreases as it proceeds into the particle core. Furthermore, a poly-crystalline particle has multiple grains with different crystal orientations and grain boundaries. Hence, it is important to choose a system with a well-defined surface to study the effect of Li flux on the initial lithiation of crystalline silicon.

In this report, structural changes of amorphous Li_xSi were investigated as a function of Li flux and total charge during the initial lithiation of single crystal (100) Si wafers using solid-state ⁷Li NMR spectroscopy. Single crystal (100) Si wafers were used as a model system in this study, as the Li flux could be precisely controlled and uniformly distributed across the surface of the wafer. This study on single crystal Si wafers compliments previous NMR studies^{26–31} on crystalline Si particles by examining the influence of Li flux and total charge on the structural changes in amorphous Li_xSi during the initial lithiation of crystalline Si.

Experimental

Si electrodes were prepared by cleaving p-type (boron doped) single crystal Si (100) wafer of 250 μ m thickness into ~ 1 cm × 1 cm squares. A 100 nm Cu film was deposited on the back side of the wafer to form a current collector that will provide uniform current density and prevent lithiation from that side. 1 M LiPF6 in 1:1:1 ethylene carbonate (EC)/diethyl carbonate (DEC)/dimethyl carbonate (DMC) was used as an electrolyte solution and a Celgard polymer film was used as a separator. Coin cells were assembled in an Ar filled glove box with Si as working and Li foil as counter/reference electrodes. The cells were cycled using a Solartron 1470E potentiostat. During lithiation, a Si will react with the Li ions to create a Li_xSi phase that will uniformly propagate from the front (the side facing the Li) into

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Figure 1. Sample packing and configuration between sample and external magnetic field for (a) angle resolved static NMR and (b) MAS NMR.

the bulk Si wafer with a thickness proportional to the total charge of the sample.

To investigate the effect of the Li flux (defined as a current density in μ A/cm²) and total charge on the structural changes, the Si electrodes were lithiated at constant current densities of 25 μ A/cm², 50 μ A/cm², 100 μ A/cm² and 200 μ A/cm² for 24 hours and 48 hours (denoted by 25 μ A24 h to 200 μ A48 h). Different lithiation hours gave different total charges at a given current density (e.g. 25 μ A24 h vs. 25 μ A48 h) and twice the current density at half the lithiation hour had the same total charges at different current densities (e.g. 25 μ A48 h) vs. 50 μ A24 h).

After finishing the initial lithiation of single crystal Si, coin cells were immediately disassembled and the lithiated Si squares were washed with DMC in the glove box. The washed lithiated Si squares were then cut into 3–4 mm by 6–10 mm pieces and transferred into a 7 mm air-tight NMR sample rotor for angle resolved static NMR measurements. Both angle resolved static NMR and magic angle spinning (MAS) spectra were taken for each lithiated Si wafer using the air-tight NMR sample rotors. For MAS NMR measurements, the lithiated Si pieces were cut into smaller pieces (1–3 mm by 1–3 mm) and horizontally stacked in a rotor together with inert SiO₂ particles to help the magic angle spinning (Fig. 1). A ground sample was also made by grinding a lithiated silicon wafer in the glove box using a porcelain pestle and mortar.

Solid-state ⁷Li NMR measurements were carried out with a Bruker DSX 300 spectrometer (7T magnetic field and 116.64 MHz resonance frequency) using both angle resolved and magic angle spinning double resonance probes. For static NMR measurements, the angle between the external magnetic field and the normal direction of the Li_xSi layer (θ_n) was varied by a goniometer. The $\theta_n = 0^\circ$ and $\theta_n = 90^\circ$ when the external magnetic field is parallel and perpendicular to the normal direction of the Lix Si layer, respectively. In MAS NMR measurements, the normal direction of the Li_xSi layer in the stacked wafer pieces were parallel to the spinning axis (Fig. 1), therefore the angle of 54.7° between the field and the normal direction was kept constant during spinning at 6.8 kHz. Single pulse NMR spectra were collected with a pulse length of 4 μ s (90° pulse) for ⁷Li and a repetition delay of 0.2 s. The number of transients was $1024 \sim 64000$ times, depending on the total charge applied to the wafers. ⁷Li NMR chemical shifts were referenced by 1 M LiCl solution in D₂O at 0 ppm.

Results and Discussion

Fig. 2 shows a constant potential plateaus for the initial lithiation of a single crystal Si at various current densities indicating a reaction limited kinetics with a moving phase boundary, which is consistent with previous studies.¹⁶ It is believed that these potentials are dependent on the Li concentration at the electrolyte/electrode interface and the impedance of a specific cell. It is observed that the value of the potential plateau decreases with the increasing current density, though there may be up to a 20 mV variation for a given current density. This variation may originate from the change in the cell impedance during a long lithiation period. It should be noted that the potential plateau is observed to be very flat in 1–3 hour windows, as is reported in previous studies¹⁶ (see supporting information, S1).

The static NMR spectra (Fig. 3) show the chemical shift for the NMR resonance taken at $\theta_n = 0^\circ$ is higher than that at $\theta_n = 90^\circ$. The angular dependence of the chemical shift, $\delta(\theta_n)$, is due to a



Figure 2. Potential profiles during initial lithiation of NMR samples. There is up to 20 mV variation in the plateau values, which may be attributed to change in cell impedance.



Figure 3. Representative angle resolved static NMR spectra taken at $\theta_n = 0^\circ$ and $\theta_n = 90^\circ$.

demagnetizing field produced inside a magnetic material that cancels out an internal magnetization, known as the bulk magnetic susceptibility (BMS) effect.³² We observed that $\delta(\theta_n)$ was not affected by the orientation of the underlying crystalline Si wafer, but only to the orientation between the Li_xSi layer and the external magnetic field (see supporting information, S2).

The total field experienced by a nuclear spin in the sample can be written as

$$H_{tot} = H_{ext} + H_{int} + M + H_{demag},$$

where H_{ext} is the external field, M is the magnetization, H_{demag} is the demagnetizing field, and H_{int} is the other internal fields except for the magnetization and demagnetizing field. The demagnetizing field is strongly dependent on a sample shape, size and geometrical configuration between the external field and sample. Since the thickness of the Li_xSi layer is expected to be smaller than 50 µm in our samples (estimated from the maximum total charge applied), the Li_xSi layer can be considered as an infinite plane. It is well known in the classical electrodynamics³³ that $H_{demag} = -M$ when the normal direction of the infinite plane (i.e., the Li_xSi layer) is parallel to the external fields and $H_{demag} = 0$ when it is perpendicular to the field. Therefore, the total fields can be described as

$$H_{tot} = H_{ext} + H_{int}$$
 (at $\theta_n = 0^\circ$)

$$H_{tot} = H_{ext} + H_{int} + M$$
 (at $\theta_n = 90^\circ$).



Figure 4. Chemical shift $\delta(\theta_n)$ as a function of lithiation current density and the angle θ_n between the normal direction of Li_xSi layer and the external magnetic field.

Since the chemical shifts obtained from our study were found to be higher at $\theta_n = 0^\circ$ than at $\theta_n = 90^\circ$, the magnetization M is antiparallel to the external field, indicating that Li_xSi has diamagnetism. From $M = \chi H_{ext}$ and the chemical shift difference of 2 to 4 ppm (see supporting information, S3) between $\delta(\theta_n = 0^\circ)$ and $\delta(\theta_n = 90^\circ)$, the diamagnetic susceptibility χ is expected to be -2×10^{-6} to -4 $\times 10^{-6}$. To the best of our knowledge, this is the first experimental observation of magnetic property on the amorphous Li_xSi phases. Similar bulk magnetic susceptibility behavior was observed in a paramagnetic Li foil but with an opposite NMR shift direction.³⁴ In previous NMR measurements²⁶ on crystalline lithium silicides, the sample shape can be considered as a symmetric sphere where the demagnetizing field is $H_{demag} = -1/3M^{35}$ regardless of the external field direction. Therefore, the value $\delta_M = \delta(90^\circ) + \frac{1}{3} \{\delta(0^\circ) - \delta(90^\circ)\} (\delta_M$ stands for the chemical shift of spherical shaped particles) can be taken as the chemical shifts for the purpose of comparison with chemical shifts of crystalline lithium silicides. NMR chemical shifts plotted as a function of θ_n are given in Fig. 4 where the chemical shifts were extracted from the peak position in each individual NMR spectrum taken at different angles. Since $\delta(\theta_n)$ resembles a cosine function (Fig. 4), $\delta(\theta_n)$ has the value of $\delta_M = \delta(90^\circ) + \frac{1}{3} \{\delta(0^\circ) - \delta(90^\circ)\}$ when $\theta_n = 54.7^\circ$ (also called the magic angle).

A few selected spectra from Fig. 3 are plotted in Fig. 5 to better illustrate the chemical shift dependence on Li flux. Figure 5 clearly shows that the chemical shift decreases with the increasing of lithiation



Figure 5. An array of static NMR spectra taken at $\theta_n = 0^\circ$ and different current densities for (a) 24 h and (b) 48 h. Dashed lines are for the guide of the eye.



Figure 6. An array of MAS NMR spectra taken at 6.8 kHz spinning rate and at different current densities and charges.

current density. NMR spectra given in Figs. 3 and 5 all display a predominant single peak with a linewidth of $1.4 \sim 1.7$ kHz ($12 \sim 15$ ppm) except for 200 μ A48 h, which has a small shoulder at around 18 ppm. The linewidth of the main resonance peak is comparable with that of an individual peak of multiple resonances: ~ 1.0 kHz – 1.4 kHz for micro particles and ~ 1.0 –2.4 kHz for nano particles in previous MAS NMR studies.^{26,27} A small additional peak at around -3 ppm was observed in Figs. 3 and 5 and its intensity does not depend on the total charge. This peak may be associated with the chemical species in SEI (solid electrolyte interface) that are stuck on the wafer surface and possible broadening of quadrupole interactions in static NMR spectra.

In addition to the angle resolved static NMR measurements, MAS NMR measurements at a 6.8 kHz spinning rate were carried out to examine multiple resonance structures which may be buried in our NMR linewidth. At first, samples were ground, but we observed that the grinding process significantly affected the linewidth and peak position, possibly due to the unknown reactions induced by the grinding process (see supporting information, S4). Thus, we adapted an alternative method of horizontally stacking the small Li_xSi wafer pieces in a rotor. In this configuration, the value δ_M can be obtained directly from the peak position since θ_n is fixed to the magic angle during spinning. The observed MAS spectra are shown in Fig. 6. It should be noted that the spectra for 25 μ A24 h ~ 100 μ A24 h have an unbalanced baseline for the main peak due to asymmetric spinning side bands (see supporting information, S5). Overall the MAS NMR spec-

tra are similar to those of static NMR spectra. Most spectra except for 200 μ A48 h display a predominant single peak with a linewidth of 1.0 kHz \sim 1.3 kHz and the chemical shift is also systematically decreases with the increasing of current density. However, the shoulder component at around 18 ppm appeared in the static spectrum for 200 μ A48 h is better resolved in the MAS spectrum. This small component observed at 18 ppm is most likely the result of non-uniform lithiation under a high current density of 200 μ A/cm².

Both angle resolved static NMR and magic angle spinning (MAS) spectra for all lithiated Si wafers show a predominant single peak with a relatively narrow linewidth. The linewidths of both static and MAS spectra are similar to that of an individual peak in a spectrum of multiple peaks observed for silicon particles under the high spinning rate of 38 kHz.²⁶ This suggests that a relatively uniform phase with similar structures of Lix Si exists in the initial lithiated Si wafer and the MAS NMR spectra taken at 6.5 kHz are adequate to resolve multiple peaks that may be present in this study. Based on the chemical shifts taken for a series of known crystalline Li_xSi,²⁶ the high Li content or higher x in Li_xSi gives a lower chemical shift. This trend is clearly illustrated in the chemical shift curves $\delta(\theta_n)$ as a function of θ_n and lithiation current density (Fig. 4). The $\delta(\theta_n)$ curves taken at different total charges with the same current density (i.e. 200 μ A24 h and 200 µA48 h) coincide well with each other, whereas the curves at the same total charge with different current densities are a long way apart. Therefore, it is clear that the Li concentration is largely dependent on the lithiation current density rather than the total charge applied during the initial lithiation of single crystal Si (100) wafer.

In order to check the reproducibility of our measurement and a variation in chemical shift under a given current density, same experiments were repeated several times by making identical coin cells. A similar trend shown in Fig. 4 was found from the results of repeated experiments, and the variation in chemical shifts is not too large to change the overall trend (see supporting information, S3, and the error bar in Fig. 7. A few curves that are not matched well in Fig. 4 (e.g. $100 \,\mu\text{A24}$ h and $100 \,\mu\text{A}$ 48 h) are due to the variation of experimental reproducibility. In comparison with the chemical shifts of crystalline lithium silicides, the δ_M values taken from both static and MAS spectra are displayed in Fig. 7 as a function of the current density with its variation from the repeated experiments.

According to the previous NMR measurements on crystalline lithium silicides,²⁶ Li ions associated with a larger number of Si-Si bonds gives a higher chemical shift from $16 \sim 19$ ppm (i.e. Li₇Si₁₂ and Li₇Si₃), while the presence of a larger number of isolated Si ions gives the lower chemical shift, e.g. 6 ppm for Li₁₅Si₄ without Si-Si bonds. The chemical shift of 11 ppm for Li₁₃Si₄ that contains both



Figure 7. Chemical shift δ_M as a function of current density observed from (a) static and (b) MAS NMR measurements. Error bar means variation obtained from repeated experiments. Dashed lines correspond to the chemical shift references obtained from crystalline lithium silicides.²⁶

isolated Si and Si-Si covalent bonds is located between the lower and higher limit. It is clear that the higher ratio between the number of isolated Si with respect to that of Si-Si bonds corresponds to a lower chemical shift and higher Li concentration in LixSi. Therefore, the chemical shifts observed in this study are directly correlated with the Si/Si-Si ratio and Li concentrations.

The initial lithiation of crystalline silicon depends on three processes: the redox reaction at the electrolyte/lithiated silicon interface, the diffusion of lithium through the lithiated phase and the chemical reaction at the reaction front, an interface between lithiated and crystalline silicon.¹⁶ Varying Li_xSi structures observed in this study suggests that the value of x in Li_xSi is not fixed at ~ 3.5 ,^{15–17,24-} depending on the Li flux. However, the value of x is independent of total charge for a given Li flux. At a higher Li flux, more Si-Si bonds are broken at the reaction front for a given surface area and a given time, giving rise to a larger Si/Si-Si ratio or a higher x in Li_xSi. On the other hand, for a given Li flux and higher total charge (or increased lithiation time,), the ratio of Si/Si-Si or the x in LixSi remains unchanged due to the moving phase boundary toward the crystalline Si as more Li ions are inserted into the Si electrode.

Since micro and nano crystalline Si electrodes were used in previous NMR and XRD¹⁵ studies, the effective Li flux is not uniform on all particles due to the varying particle sizes and shapes, and distances from particles to the current collector. Therefore, the information on the structural changes in Li_xSi as a function of Li flux and total charge obtained from this study is useful for future modeling of the reaction front kinetics and helps the understanding of the kinetics and mechanisms at the reaction front. However, a thorough description of kinetics at the reaction front requires future studies involving in-situ and time dependent measurements for the initial lithiation of crystalline silicon.

Conclusions

In this report, structural changes in amorphous LixSi were investigated as a function of Li flux and total charge during the initial lithiation of single crystal (100) Si wafers using solid-state ⁷Li NMR spectroscopy. A single crystal Si wafer was used as a model system in the study because of well-controlled Li flux uniformly distributed across the surface of a Si (100) wafer. The lithiated Si wafers were produced electrochemically in a coin cell configuration consisting of Si (100) wafer and Li foil as a working electrode and counter/reference electrode, respectively. The initial lithiation of the single crystal Si wafers was achieved galvanostatically at different rates on the coin cells. Both angle resolved static NMR and MAS spectra for each lithiated Si wafer show a predominant single peak with a relatively narrow linewidth, indicating uniform structures of LixSi. In addition the observed chemical shift systematically decreases with increasing lithiation current density or Li flux, indicating that a higher Li flux results in a higher Li concentration in Li_xSi during the initial lithiation of single crystal Si. It was also observed that the structure of Li_xSi or x in Li_xSi is fixed regardless of the total charge applied at a given Li flux. The results from this study help a better understanding of the kinetics, the reaction mechanisms and the theoretical modeling of the reaction kinetics at the reaction front in the initial lithiation.

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